

MODELING DOSE EFFECT AND CYCLE EFFECT IN DOSE FINDING STUDIES OF TARGETED AGENTS

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Epiclin 05/15/19



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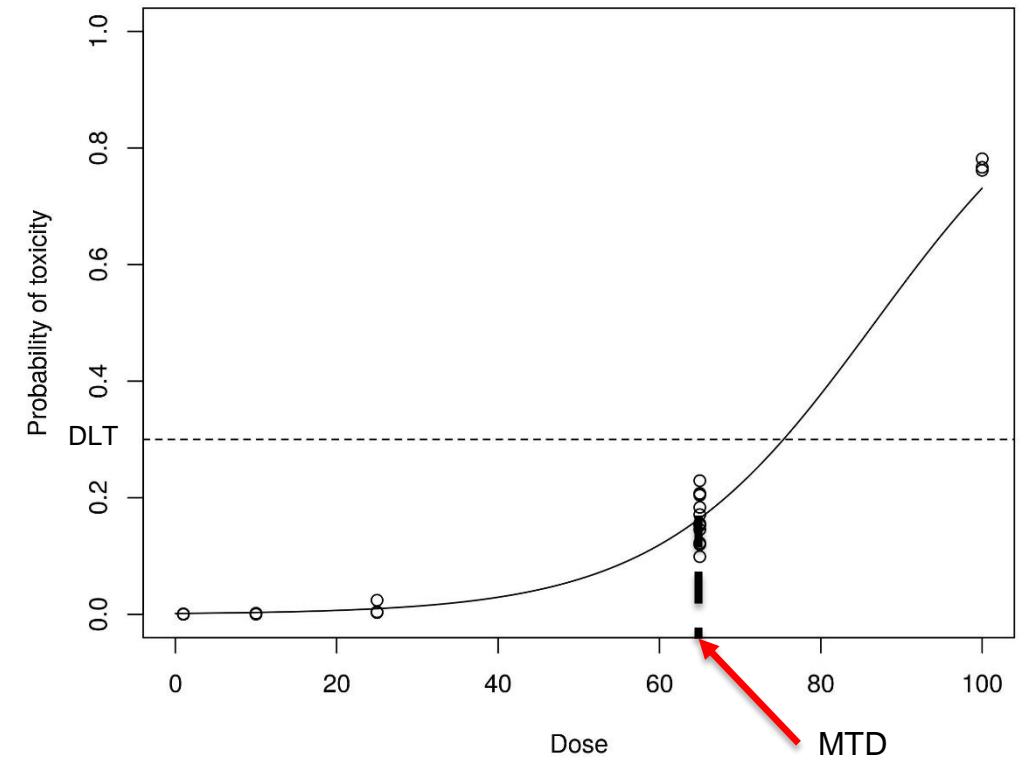
Motivation

Phase I trial objective:

Assessing drug safety finding the maximum tolerated dose (MTD) before Phase II & III efficacy trials

Standard adaptive designs for dose allocation:

- 3+3
- Continual reassessment method¹ (CRM)



Evaluation criteria = % of dose limiting toxicity (DLT = **Toxicity grade ≥ 3**) at **1st cycle**

Appropriate criteria for conventional cytotoxic therapy

But...

Motivation

Temporal evolution, especially relevant for long term toxicity:

- Targeted therapy: **late** severe toxicities or **persistent low grade toxicities**

European Medical Agency recommendations:

“**Lower grade toxicity** **over longer periods** of time that affect tolerability and the possibility of maintaining the intended dose intensity may need to be addressed in the DLT and MTD definitions”

Need to consider a **finer scale of toxicity intensity** and **temporal evolution** of toxicities

Motivation

More informative model considering **all toxicity grades** (= ordinal variable):

- Continuation ratio (CR) model based continuous reassessment method (CRM) design² (CR-CRM)

More complex than the standard binary CRM but similar dose finding performance than classical binary CRM design

Continuation ratio model

Given that a patient experiment a toxicity of grade k , which is the expected increase of his odds of more severe toxicity with dose?

Toxicity grade k	0	1	2	≥ 3	

$$P(Y_i > k | Y_i \geq k) = \text{logit}^{-1}(\beta_k + \gamma D_i)$$

$$P(Y_i > 0 | Y_i \geq 0) = \text{logit}^{-1}(\beta_0 + \gamma D_i)$$

$$P(Y_i > 1 | Y_i \geq 1) = \text{logit}^{-1}(\beta_1 + \gamma D_i)$$

$$P(Y_i > 2 | Y_i \geq 2) = \text{logit}^{-1}(\beta_2 + \gamma D_i)$$

With $\exp(\gamma) = \text{Odd Ratio}$

Low number of patients → Proportional odds (PO) assumption required for stable results

Reasonable assumption?

Objectives

Essential to validate the PO assumption before further developments

Idea: Pooled analysis of 54 phase I clinical trials ↗ ↗ information to:

- **Verify plausibility of PO assumptions for dose**
- **Consider other untapped information:**
 - **Cycle** (log linear effect + verify plausibility of PO assumption)
 - Heterogeneous mechanisms between types of toxicity?

Material

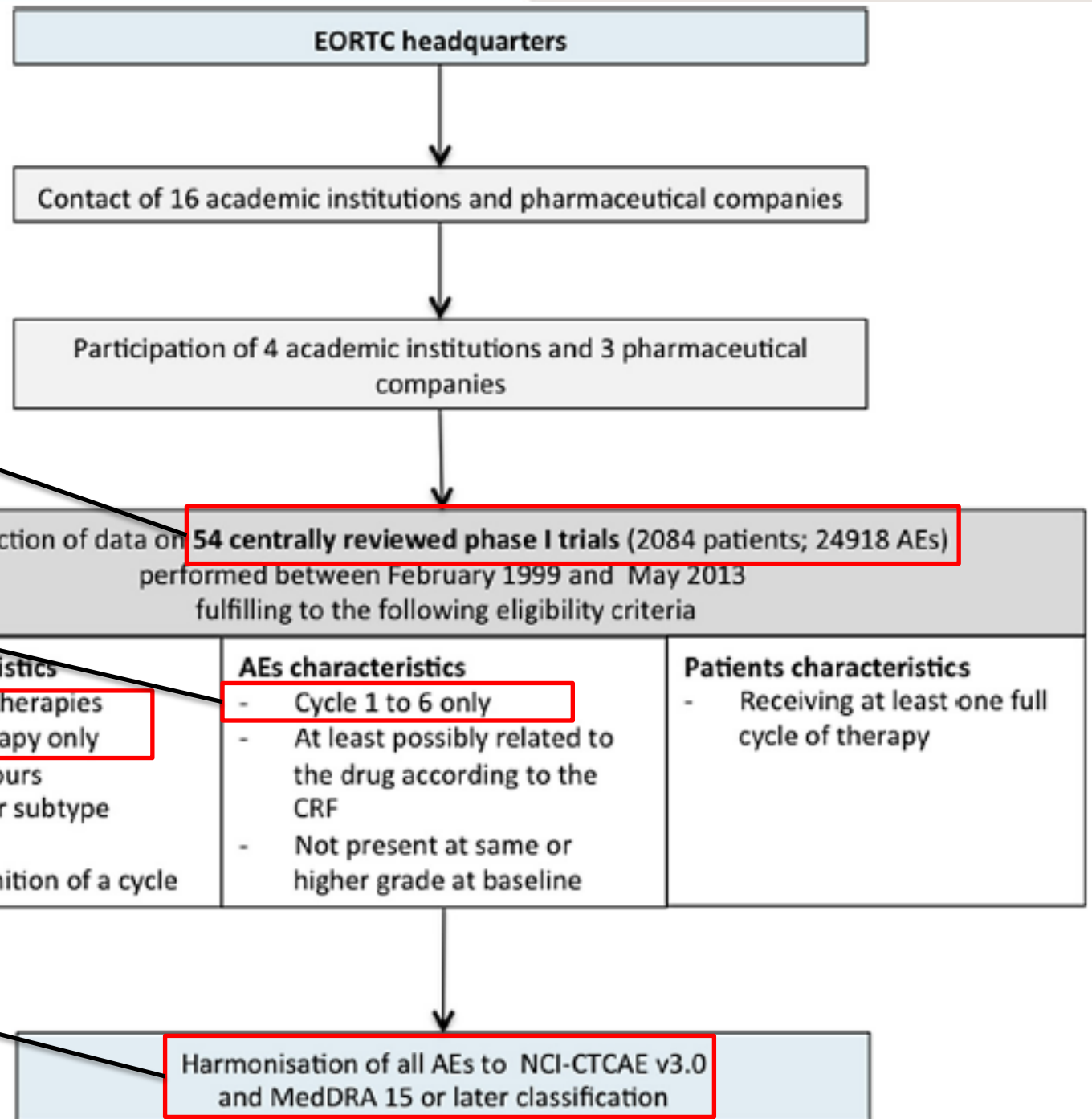
Source: Postel-Vinay et al. 2014³

Standardization

Repeated
measurement

Single agent (avoid
confusion and synergic
effect)

Toxicity grades defined
according to NCI scales



Material

- Most severe grade of type of toxicity j experienced by the patient i at the t^{th} cycle:

$$Y_{i,j,t} = \begin{cases} 0 & \text{No toxic response} \\ 1 & \text{Experience of grade 1 toxicity} \\ 2 & \text{Experience of grade 2 toxicity} \\ 3 & \text{Experience of DLT (grade } \geq 3 \text{ toxicity)} \end{cases}$$

- Different types of toxicity (total = 9,904 for 2,048 patients):

Grade	Cutaneous	Digestive	General disorder	Hematologic	Other	Total
1	549	1,754	403	1,344	1,513	5,563
2	207	794	433	748	946	3,128
≥ 3	31	190	345	200	447	1,213
Total	787	2,738	1,181	2,292	2,906	9,904

Statistical model

Multivariate CR model (proportional odds):

Patient specific multivariate random effect (for each toxicity type)

$$\alpha_{ij} \sim \text{MVN}(\mathbf{0}, \Sigma)$$

Toxicity type specific intercept

Standardized dose:

$$D_i = \frac{\text{Planned dose}_i}{\text{MTD}_{\text{study}_i}}$$

Cycle number of the t^{th} observation of the patient i

$$P(Y_{ijt} > k | Y_{ijt} \geq k) = \text{logit}^{-1}(\alpha_{ij} + \beta_{jk} + \gamma_j D_i + \vartheta_j C_{ijt})$$

$$\rightarrow \begin{cases} P(Y_{ijt} > 0 | Y_{ijt} \geq 0) = \text{logit}^{-1}(\alpha_{ij} + \beta_{j0} + \gamma_j D_i + \vartheta_j C_{ijt}) \\ P(Y_{ijt} > 1 | Y_{ijt} \geq 1) = \text{logit}^{-1}(\alpha_{ij} + \beta_{j1} + \gamma_j D_i + \vartheta_j C_{ijt}) \\ P(Y_{ijt} > 2 | Y_{ijt} \geq 2) = \text{logit}^{-1}(\alpha_{ij} + \beta_{j2} + \gamma_j D_i + \vartheta_j C_{ijt}) \end{cases}$$

Proportional odd for dose

Proportional odd for cycle

Statistical model

Multivariate CR model (non-proportional odds):

$$P(Y_{ijt} > k | Y_{ijt} \geq k) = \text{logit}^{-1} \left(\alpha_{ij} + \beta_{jk} + \left(\sum_{m=0}^{k-1} \gamma_{jm} \right) D_i + \left(\sum_{m=0}^{k-1} \vartheta_{jm} \right) C_{ijt} \right)$$

$$\rightarrow \begin{cases} P(Y_{ijt} > 1 | Y_{ijt} \geq 0) = \text{logit}^{-1}(\alpha_{ij} + \beta_{j0} + \gamma_{j0}D_i + \vartheta_{j0}C_{ijt}) \\ P(Y_{ijt} > 1 | Y_{ijt} \geq 1) = \text{logit}^{-1}(\alpha_{ij} + \beta_{j1} + (\gamma_{j0} + \gamma_{j1})D_i + (\vartheta_{j0} + \vartheta_{j1})C_{ijt}) \\ P(Y_{ijt} > 2 | Y_{ijt} \geq 2) = \text{logit}^{-1}(\alpha_{ij} + \beta_{j2} + (\gamma_{j0} + \gamma_{j1} + \gamma_{j2})D_i + (\vartheta_{j0} + \vartheta_{j1} + \vartheta_{j2})C_{ijt}) \end{cases}$$

For K types of toxicity, PO if: for dose: $1_{\gamma_{j1} \neq 0} + 1_{\gamma_{j2} \neq 0} = 0$
for cycle: $1_{\vartheta_{j1} \neq 0} + 1_{\vartheta_{j2} \neq 0} = 0$

Statistical model: Bayesian inference

Aim: Statistical model able to generalize to future trial → predictive model

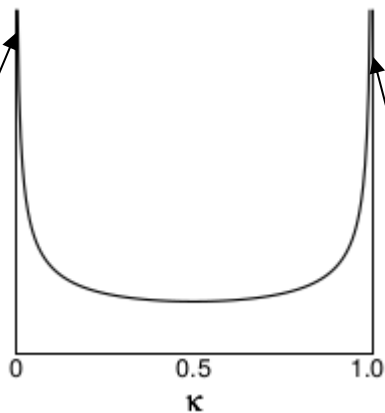
Prior for fixed effects:

Bayesian model averaging too computationally demanding → approximation using sparse model using the global-local mixture shrinkage horseshoe prior⁴

κ density

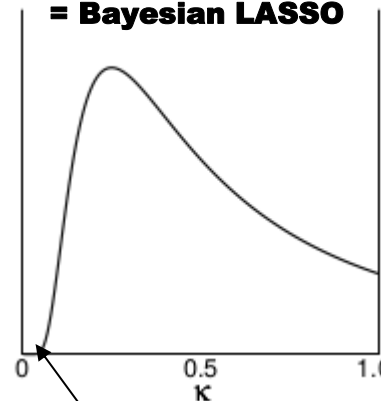
HS mimics
BMA⁴

Horseshoe



Laplacian

= Bayesian LASSO



Shrinkage parameter
formulation:

$$\bar{\theta} = (1 - \kappa)\hat{\theta}$$

Posterior
mean of θ

Maximum
likelihood
solution of θ

Expected weak shrinkage of strong θ s (small bias) Expected strong shrinkage of weak θ s

No low shrinkage
→ Bias for all estimators

Statistical model: Bayesian inference

Prior for random effects correlation matrix: LKJ prior⁵

Sampling: Hamiltonian Monte Carlo⁶ (using Stan⁷, 4 chains, 5,000 iterations including 1,000 burning)

Model comparison (PO vs non PO models): Widely applicable information criterion⁸ (WAIC)

- Averaging over the full posterior instead of rely on a single point estimation as for AIC or DIC
- Asymptotically equal to the leave-one-out cross-validation

Results

Odds ratio [95% credible interval] for dose

	Cutaneous	Digestive	General disorders	Hematologic	Others
Dose ($\exp(\gamma_{j0})$)	3.11 [2.35; 3.87]	2.58 [2.19; 2.95]	2.55 [2.12; 3.00]	3.13 [2.31; 4.01]	2.77 [2.36; 3.17]
Cycle ($\exp(\vartheta_{j0})$)	0.33 [0.23; 0.42]	0.01 [-0.04; 0.06]	0.03 [-0.02; 0.09]	0.06 [-0.01; 0.15]	0.12 [0.07; 0.17]

- Increase of the severity of toxicity with dose
- Slight increase with cycle only for cutaneous and other types of toxicity

Comparison with non PO model:

WAIC_{PO} = 31, 432.10 WAIC_{nonPO} = 30, 911.58 Difference = 520,52 (+ 1,7% for PO)

- Small decrease of patient toxicity risk prediction performance for PO model
- Deviance from PO assumption?

Results

$$\begin{aligned}
 P(Y_{ijt} > 1 | Y_{ijt} \geq 0) &= \text{logit}^{-1}(\alpha_{ij} + \beta_{j0} + \gamma_{j0} D_i + \vartheta_{j0} C_{ijt}) \\
 P(Y_{ijt} > 1 | Y_{ijt} \geq 1) &= \text{logit}^{-1}(\alpha_{ij} + \beta_{j0} + (\gamma_{j0} + \gamma_{j1}) D_i + (\vartheta_{j0} + \vartheta_{j1}) C_{ijt}) \\
 P(Y_{ijt} > 2 | Y_{ijt} \geq 2) &= \text{logit}^{-1}(\alpha_{ij} + \beta_{j0} + (\gamma_{j0} + \gamma_{j1} + \gamma_{j2}) D_i + (\vartheta_{j0} + \vartheta_{j1} + \vartheta_{j2}) C_{ijt})
 \end{aligned}$$

Odds ratio [95% credible interval] for dose

	Cutaneous	Digestive	General disorders	Hematologic	Others
$\exp(\gamma_{j0})$ Grade 0 $\rightarrow \geq 1$	2.98 [2.27; 3.96]	2.35 [1.96; 2.72]	2.16 [1.77; 2.65]	2.87 [2.17; 3.75]	2.51 [2.12; 2.98]
$\exp(\gamma_{j1})$ Grade 1 $\rightarrow \geq 2$	0.06 [-0.41; 0.43]	0.22 [-0.06; 0.51]	0.37 [0.10; 0.67]	0.30 [-0.01; 0.72]	0.08 [-0.19; 0.38]
$\exp(\gamma_{j2})$ Grade 2 $\rightarrow \geq 3$	0.33 [-0.56; 1.41]	1.37 [0.84; 1.87]	0.67 [0.05; 1.23]	0.03 [-0.37; 0.42]	0.26 [-0.03; 0.58]

→ PO assumption reasonable, excepting for digestive and general disorder toxicities

Results

$$\begin{aligned} P(Y_{ijt} > 1 | Y_{ijt} \geq 0) &= \text{logit}^{-1}(\alpha_{ij} + \beta_{j0} + \gamma_{j0} D_i + \vartheta_{j0} C_{ijt}) \\ P(Y_{ijt} > 1 | Y_{ijt} \geq 1) &= \text{logit}^{-1}(\alpha_{ij} + \beta_{j0} + (\gamma_{j0} + \gamma_{j1}) D_i + (\vartheta_{j0} + \vartheta_{j1}) C_{ijt}) \\ P(Y_{ijt} > 2 | Y_{ijt} \geq 2) &= \text{logit}^{-1}(\alpha_{ij} + \beta_{j0} + (\gamma_{j0} + \gamma_{j1} + \gamma_{j2}) D_i + (\vartheta_{j0} + \vartheta_{j1} + \vartheta_{j2}) C_{ijt}) \end{aligned}$$

Odds ratio [95% credible interval] for cycle

	Cutaneous	Digestive	General disorders	Hematologic	Others
$\exp(\vartheta_{j0})$ Grade 0 $\rightarrow \geq 1$	0.37 [0.27; 0.48]	0.04 [-0.01; 0.11]	0.07 [0.01; 0.14]	0.08 [-0.00; 0.17]	0.18 [0.11; 0.24]
$\exp(\vartheta_{j1})$ Grade 1 $\rightarrow \geq 2$	-0.16 [-0.33; -0.02]	-0.08 [-0.17; 0.00]	-0.08 [-0.17; -0.00]	-0.02 [-0.12; 0.05]	-0.09 [-0.17; -0.00]
$\exp(\vartheta_{j2})$ Grade 2 $\rightarrow \geq 3$	0.05 [-0.20; 0.37]	-0.01 [-0.13; 0.11]	-0.08 [-0.26; 0.06]	0.00 [-0.10; 0.12]	-0.09 [-0.20; 0.01]

Small cycle effect
with attenuation for grade > 1

No cycle effect or attenuation?

Results

Random effect correlation matrix [95% credible intervals]

	Cutaneous	Digestive	General disorders	Hematologic	Others
Cutaneous	1	0.22 [0.15; 0.28]	0.05 [-0.01; 0.12]	-0.18 [-0.27; -0.07]	0.01 [-0.06; 0.08]
Digestive		1	0.45 [0.40; 0.51]	0.28 [0.23; 0.35]	0.42 [0.36; 0.46]
General disorders			1	0.26 [0.21; 0.33]	0.41 [0.36; 0.46]
Hematologic				1	0.37 [0.32; 0.43]
Others					1

Low correlation

Moderate correlation: vomiting and pain
(digestive disorder) tires (General disorders) a lot

Low to moderate correlation between random effects

➤ **Provide different information**

Discussion

P1 data not fully exploited: More detailed toxicity intensity definition and temporal aspects could be considered

Low correlation and heterogeneous results between the different type of toxicity:

➤ **Complementary information → useful for patient management**

Slight loss of patient risk prediction performance using PO model:

- **PO assumption questionable for digestive and general disorder toxicities**
 - Discourage the CR-CRM design for study with large expected proportion of these types of toxicity
- **Cycle effect not clear:**
 - Distinction between time and cumulative dose?
 - More investigation on its functional form (other than log-linear) should be performed

Acknowledgment

Grant from:
INCa (French NCI) Optidose-immo



Ligue nationale contre le cancer, meta analysis hub



Data providing:
Laurence Collette, EORTC-HQ,
Belgium, DLT-TARGETT group

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